

5.4 Factoring Special Polynomials

When we multiply a binomial by itself, we square the binomial. The result is a polynomial called the perfect square trinomial.

Examples:

$$(a + 4)^2 = (a + 4)(a + 4)$$

$$(t - 3)^2 = (t - 3)(t - 3) = t^2 - 6t + 9$$

$$(5n + 3)^2 = (5n + 3)(5n + 3) = 25n^2 + 30n + 9$$

Each trinomial is a perfect square trinomial!

There are special binomial products that produce binomials. The result is a polynomial called difference of squares.

Examples:

$$\begin{aligned} (x + 4)(x - 4) &= x^2 - 4x + 4x - 16 \\ &= x^2 - 16 \end{aligned}$$

$$\begin{aligned} (5n + 3)(5n - 3) &= 25n^2 - 15n + 15n - 9 \\ &= 25n^2 - 9 \end{aligned}$$

Each binomial result is a difference of squares!

Two rules about factoring special polynomials you should know:

1. Perfect square trinomials, $a^2 + 2ab + b^2$ and $a^2 - 2ab + b^2$, factor into $(a + b)^2$ and $(a - b)^2$, respectively;
2. Difference of squares, $a^2 - b^2$, factor into $(a + b)(a - b)$.

Example 1: Factoring Difference of Squares

Factor each binomial, if possible.

a) $x^2 - 64$

b) $4v^2 - 49$

c) $7a^3b^2 - 28a^5$

c) $x^2 - 100$

d) $25h^2 - 81$

Example 2: Factoring Perfect Square Trinomials

Factor each trinomial

a) $x^2 + 6x + 9$

b) $25n^2 + 20n + 4$

c) $r^2 + 6r + 9$

d) $9m^2 - 12m + 4$

Homework:

P. 246 # 1(ALL)

#2 – 7 (pick 3)

#8 – 11

#13, 15, 17